

It is possible that even though the gauche transition state (5) does not involve intramolecular hydrogen bonding, it may preferentially lead to the solvate ($\text{CH}_3\text{CH}_2\text{O}\cdot\text{H}_2\text{O}$); however, the experimental studies indicate that the ethoxide-water complex is the major product,^{7c,8} whereas the theoretical studies predict that the gauche elimination should have a significantly larger barrier (5.2 kcal/mol) than the antiperiplanar elimination. Additional evidence against competing pathways is found in the calculated vibrational frequencies. On the basis of zero-point energy differences, the calculations predict that the barriers for both the antiperiplanar and gauche eliminations of $\text{CD}_3\text{CD}_2\text{OCH}_3$ are about 1.1 kcal/mol above those of $\text{CH}_3\text{CH}_2\text{OCH}_3$, and therefore both pathways should give similar kinetic isotope effects.^{32,33} Our calculated differences in transition state barriers are in good accord with Bierbaum and Bowers' earlier estimate.^{7c} Using their statistical rate model and the observed kinetic isotope effects, they predicted that the barrier in $\text{CD}_3\text{CD}_2\text{OCD}_2\text{CD}_3$ is 1.1 kcal/mol greater than that in $\text{CH}_3\text{CH}_2\text{OCH}_2\text{CH}_3$. Given the present theoretical results, it seems unlikely that a cyclic transition state is involved in the gas-phase reactions of HO^- with ethers, and therefore another explanation must be found for the different isotope effects observed in the two product channels. Although it is not completely consistent with the energy dependence that de Koning and Nibbering reported,⁸ a rational explanation is that the reaction involves only an antiperiplanar pathway³⁴ and that a second isotope effect is

active in the partitioning between solvated and unsolvated products.

Conclusions

For β -elimination reactions with a high degree of E1_{cb} -like character, the preference for periplanarity is greatly reduced. Because the carbon-leaving group bond is hardly broken in the transition state, there is little advantage to hyperconjugation and partial π -bond formation. As a result, steric effects can become important in determining the preferred conformation. Synperiplanar transition states are only possible when the advantage of conjugation outweighs the steric disadvantages of an eclipsed conformation. In E1_{cb} -like reactions, this is not necessarily true and gauche transition states are possible. These effects are almost perfectly balanced in the reaction of HO^- with $\text{CH}_3\text{CH}_2\text{OCH}_3$ where a gauche transition state is slightly more stable than a synperiplanar transition state. This highlights the fact that in E1_{cb} -like syn eliminations, the transition state barrier is relatively insensitive to the torsional angle ($\text{H}_\beta\text{-C}_\beta\text{-C}_\alpha\text{-X}$). However, antiperiplanar transition states generally are preferred for gas-phase β -eliminations because they allow for conjugation within a staggered conformation. Further studies on the effect of substitution in E2 transition states have been completed and will be published subsequently.³⁵

Acknowledgment. We thank the Chemical Instrumentation Program of the National Science Foundation (CHE-8822716) for providing the funds to purchase the Multi-Flow-Trace14 computer used for these calculations.

Registry No. Hydroxide, 14280-30-9; ethyl methyl ether, 540-67-0.

Supplementary Material Available: Listing of Z-matrix elements, energies, frequencies, and reaction coordinates (10 pages). Ordering information is given on any current masthead page.

(31) In all previous theoretical studies of E2 eliminations, nearly linear proton transfer geometries ($\text{base-H}_\beta\text{-C}_\beta$) have been observed (see ref 2, 3, 6).

(32) The zero-point-energy differences predict a smaller isotope effect for the antiperiplanar and gauche eliminations of the (HO^- - $\text{DCH}_2\text{CH}_2\text{OCH}_3$) system (a transition state barrier difference of about 0.8 kcal/mol compared to the all hydrogen substrate). Therefore, both primary and secondary isotope effects are important in these reactions. Experimentally, de Koning and Nibbering have noted this result; see ref 8.

(33) Attempts to analyze the theoretical results with a simple RRKM dynamics approach (see ref 27a) led to unrealistically low rates and exceptionally large $k_{\text{H}}/k_{\text{D}}$ values. Undoubtedly these errors result from treating low-frequency vibrations as harmonic oscillators rather than as hindered rotors (the differences cannot be explained solely on the basis of errors in the calculated barrier). Although beyond the scope of the present study, a more sophisticated dynamics treatment is appropriate for a system that is characterized by many low-frequency vibrations and the possibility of tunnelling (see ref 27c-e).

(34) Although entropy may slightly favor the gauche elimination (the small torsional barrier and the presence of two gauche pathways should increase the entropy), the large difference in activation energy (5.2 kcal/mol) should ensure that antiperiplanar eliminations dominate.

(35) Syn-gauche transition states have been observed in other systems, and the borderline between synperiplanar and syn-gauche transition states has been investigated: Gronert, S. Manuscript in preparation.

Ab Initio Calculations on Silicon Analogues of the Allyl Radical

Michael B. Coolidge,[†] David A. Hrovat, and Weston Thatcher Borden*

Contribution from the Department of Chemistry, University of Washington, Seattle, Washington 98195. Received April 8, 1991

Abstract: Calculations at the CI-SD/6-31G* level of theory have been performed in order to determine the effect on the A-H bond dissociation energy (BDE) in X-AH_3 ($\text{A} = \text{C}$ and $\text{A} = \text{Si}$) of replacing $\text{X} = \text{H}_2\text{C}-$ by $\text{X} = \text{H}_2\text{C}=\text{CH}-$ and $\text{H}_2\text{Si}=\text{CH}-$ and of replacing $\text{X} = \text{H}_3\text{Si}-$ by $\text{X} = \text{H}_2\text{C}=\text{SiH}-$ and $\text{H}_2\text{Si}=\text{SiH}-$. The conjugative stabilization energies (CSEs) of the resulting allylic radicals have been obtained from the energies calculated to be required to twist a terminal AH_2^* group out of conjugation. Except for $\text{X} = \text{H}_2\text{C}=\text{CH}-$ and $\text{H}_2\text{Si}=\text{CH}-$ in X-CH_2^* , these two definitions of allylic resonance energy give nearly identical values. The reason for the calculated difference between $-\Delta\text{BDE}$ and CSE in $\text{H}_2\text{C}=\text{CH-CH}_2^*$ and in $\text{H}_2\text{Si}=\text{CH-CH}_2^*$ is discussed. It is also found that, with the exception of $\text{H}_2\text{Si}=\text{CH-SiH}_2^*$, the calculated allylic resonance energies are generally those expected from the π BDEs in $\text{H}_2\text{C}=\text{CH}_2$, $\text{H}_2\text{C}=\text{SiH}_2$, and $\text{H}_2\text{Si}=\text{SiH}_2$. It is shown that pyramidalization at silicon lowers the resonance energy of $\text{H}_2\text{Si}=\text{CH-SiH}_2^*$ from that expected, based on the strength of the C-Si π bond in $\text{H}_2\text{C}=\text{SiH}_2$.

The results of ab initio calculations show that substituents, X, affect the A-H bond dissociation energy (BDE) of X-AH_3 differently, depending on whether A is carbon or silicon.¹ For $\text{A} = \text{C}$, as well as for $\text{A} = \text{Si}$, X groups that can delocalize the unpaired electron in the X-AH_2^* radical tend to lower the A-H

BDE. However, since carbon forms stronger π bonds than silicon,² conjugative stabilization of the radical formed by breaking the A-H bond is generally found to be more important for $\text{A} = \text{C}$ than for $\text{A} = \text{Si}$.

[†] Present address: Frank J. Seiler Research Laboratory, U.S. Air Force Academy, USAFA, Colorado 80840-8628.

(1) Coolidge, M. B.; Borden, W. T. *J. Am. Chem. Soc.* 1988, 110, 2298.
(2) Review: Kutzelnigg, W. *Angew. Chem., Int. Ed. Engl.* 1984, 23, 272.

Table I. CI-SD/6-31G* Energies Calculated at (U)HF/6-31G* Geometries

X	X-AH ₃		X-AH ₂ ^a		X-AH ₂ ^b	
	A = C	A = Si	A = C	A = Si	A = C	A = Si
CH ₃	-79.5040	-330.5020	-78.8490	-329.8678		
H ₂ C=CH	-117.4470	-368.4434	-116.8142	-367.8098	-116.7898	-367.8095
H ₂ Si=CH	-368.4122	-619.4223		-618.7896	-367.7596	-618.7884
SiH ₃	-330.5020	-581.4909	-329.8491	-580.8624		
H ₂ C=SiH	-368.4255	-619.4191	-367.7862	-618.7920	-367.7731	-618.7914
H ₂ Si=SiH	-619.4222	-870.4226		-869.8036	-618.7703	-869.7947

^aAH₂^{*} group conjugated with the π bond in unsaturated X groups. ^bAH₂^{*} group rotated out of conjugation with the π bond in X.

Our calculations revealed an important effect of substituent electronegativity on the A-H BDE in X-AH₃. For both A = C and A = Si, the A-H BDE was found to increase with the electronegativity of X. Substituent electronegativity affects the A-H BDEs in this way because the amount of s orbital character in the A-H bond of X-AH₃ increases with the electronegativity of X.³ Since, especially for π electron donating substituent groups, conjugative stabilization of X-SiH₂^{*} is of relatively minor importance, compared to conjugative stabilization of X-CH₂^{*}, substituent electronegativity has a very strong effect on the strengths of Si-H bonds.¹

Our previous study was confined to substituents that were either π electron donor groups (e.g., NH₂) or π electron acceptor groups (e.g., BH₂) but that did not themselves contain π bonds. Although it is well known experimentally that the π bonds that are present in vinyl and phenyl substituents result in the BDEs of allylic and benzylic C-H bonds being 12–14 kcal/mol lower than the C-H BDEs in saturated molecules,⁴ the Si-H BDE is apparently unaffected by the presence of an adjacent phenyl group.⁵ Moreover, the EPR spectra of both 1-silaallylic⁶ and 1-silabenzyl⁷ radicals show the unpaired spin density to be largely, though not completely, localized on silicon.

The present computational study was motivated by the desire to understand in detail the effect of an adjacent π bond on C-H and Si-H BDEs. We also wanted to compare the computed barriers to rotation and spin densities in the resulting allylic and silaallylic radicals. For completeness, our study included, in addition to vinyl, both possible silavinyl substituents and also disilavinyl. Herein we report the results of our calculations.

Computational Methodology

Geometries were optimized⁸ with RHF calculations for closed-shell molecules and with UHF calculations for radicals, using the 6-31G* basis set.⁹ For allylic and other radicals in which delocalized wave functions are a possibility, UHF calculations are preferred to ROHF calculations for geometry optimizations.¹⁰ In order to obtain energies that contain the effects of electron correlation, CI-SD calculations were performed at the RHF and UHF optimized geometries.

CI-SD calculations, which give pure doublet wave functions for radicals, are preferable to UMP calculations, which do not. The latter are based on the application of Møller-Plesset perturbation theory¹¹ to UHF

Table II. Calculated (CI-SD/6-31G*) Decreases in A-H Bond Dissociation Energies (-ΔBDEs) Caused by Unsaturated Substituents, X, in X-AH₃ and Calculated (CI-SD/6-31G*) Conjugative Stabilization Energies (CSEs) in X-AH₂^{*} (kcal/mol)

X	-ΔBDE (X-AH ₃) ^a		CSE (X-AH ₂ [*])	
	A = C	A = Si	A = C	A = Si
CH ₃	0	0		
H ₂ C=CH	13.9 ^b	0.4 ^b	15.3	0.2
H ₂ Si=CH	33.0 ^b	0.9 ^b	31.5	0.8
SiH ₃	0	0		
H ₂ C=SiH	8.5 ^c	0.9 ^c	8.2	0.4
H ₂ Si=SiH	14.2 ^c	6.0 ^c	13.6	5.6

^aA positive value indicates a lowering of the A-H BDE. ^bBDE relative to X = CH₃. ^cBDE relative to X = SiH₃.

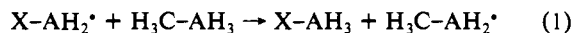
wave functions, and UMP calculations tend to give correlated wave functions which still contain the higher spin states that contaminate UHF wave functions.¹² Spin contamination is especially severe in the UHF wave functions for allylic radicals. In the UHF wave functions for the radicals studied by us, S² ranges from 0.97 for allyl to 1.31 for trisilaallyl. For a pure doublet wave function S² is 0.75.

Geometries were optimized and energies were calculated with the Gaussian 86 package of ab initio programs.¹³ Spin population analyses on the CI-SD wave functions were obtained with MELDF,¹⁴ which projects populations computed with a split-valence basis set onto an equivalent minimal basis set,¹⁵ thus facilitating analysis. Because of the large number of configurations involved in the CI-SD calculations, perturbation theory was used to select the most important configurations for the MELDF population analyses. The CI-SD wave functions were truncated so that less than 5% of the correlation energy was lost.

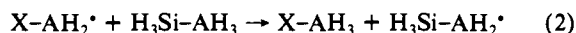
Results and Discussion

Table I gives the energies computed at the CI-SD level with the 6-31G* basis set. From the CI-SD energies the calculated amount by which various substituents, X, reduce the A-H BDE in X-AH₃ were obtained for A = C and A = Si. The reductions in BDEs are given in Table II, relative to X = H₃C- and X = H₃Si-. We have discussed previously the effect on the BDE's of methane and silane of replacing a hydrogen with a methyl or a silyl group.^{1,16}

The -ΔBDEs in Table II are actually the energies for the reactions



and



depending on whether substituent X has carbon or silicon attached to atom A. Since the reactions in eqs 1 and 2 are isodesmic,

(12) Gill, P. M. W.; Pople, J. A.; Radom, L.; Nobes, R. *J. Chem. Phys.* **1988**, *89*, 7307.

(13) Frisch, M. J.; Binkley, J. S.; Schlegel, H. B.; Raghavachari, K.; Melius, R.; Martin, R.; Stewart, J. J. P.; Bobrowicz, F.; Rohlfing, C. M.; Kahn, L. R.; Defrees, D. J.; Seeger, R.; Whiteside, R. A.; Fox, D. J.; Fluder, E.; Pople, J. A. *GAUSSIAN 86*; Carnegie-Mellon University: Pittsburgh, PA, 1986.

(14) Developed at the University of Washington by McMurchie, L., Elbert, S., Langhoff, S., and Davidson, E. R., and modified by Feller, D., and Rawlings, D.

(15) Davidson, E. R. *J. Chem. Phys.* **1967**, *46*, 3319.

(16) Using CI-SD, rather than (U)MP4SDTQ energies,¹ we calculate that a methyl substituent lowers the C-H BDE of methane by 4.3 kcal/mol but raises the Si-H BDE of silane by 0.1 kcal/mol. In contrast, a silyl substituent lowers both A-H BDEs—that of methane by 5.6 kcal/mol and that of silane by 3.5 kcal/mol.

(3) Bent, H. A. *Chem. Rev.* **1961**, *61*, 275.

(4) Review: McMillen, D. F.; Golden, D. M. *Annu. Rev. Phys. Chem.* **1982**, *33*, 493. The most recent experiments give a value of 13.5 ± 1.1 kcal/mol for the lowering of the BDE that results from replacement of alkyl by vinyl: Roth, W. R.; Bauer, F.; Beitz, A.; Ebbrecht, T.; Wüstefeld, M. *Chem. Ber.* **1991**, *124*, 1453. Doering, W. von E.; Roth, W. R.; Bauer, F.; Boenke, M.; Breuckmann, R.; Ruhkamp, J.; Wortmann, O. *Chem. Ber.* **1991**, *124*, 1461.

(5) Walsh, R. *Acc. Chem. Res.* **1981**, *14*, 246. Wetzell, D. M.; Salomon, K. E.; Berger, S.; Brauman, J. I. *J. Am. Chem. Soc.* **1989**, *111*, 3835.

(6) Jackson, R. A.; Zarkadis, A. K. *Tetrahedron Lett.* **1988**, *29*, 3493.

(7) Sakurai, H.; Umimo, H.; Sugiyama, H. *J. Am. Chem. Soc.* **1980**, *102*, 6837.

(8) RHF and UHF optimized geometries and energies are available as supplementary material; ordering information is given on any masthead page.

(9) Hariharan, P. C.; Pople, J. A. *Theor. Chim. Acta* **1973**, *28*, 213.

(10) Unless constrained by symmetry, ROHF wave functions for radicals that are known to be delocalized exhibit localization and thus give optimized geometries that are grossly incorrect. Because UHF wave functions contain some correlation between electrons of opposite spin, they do not exhibit artificial symmetry breaking and localization. Reviews: Borden, W. T.; Davidson, E. R.; Feller, D. *Tetrahedron* **1982**, *38*, 737. Davidson, E. R.; Borden, W. T. *J. Phys. Chem.* **1983**, *87*, 4783.

(11) Møller, C.; Plesset, M. S. *Phys. Rev.* **1936**, *46*, 618. Pople, J. A.; Binkley, J. S.; Seeger, R. *Int. J. Quantum Chem.* **1976**, *S10*, 1.

cancellation of errors makes the relative BDEs in Table II more accurate than the absolute A-H BDEs computed at the CI-SD/6-31G* level.¹⁷

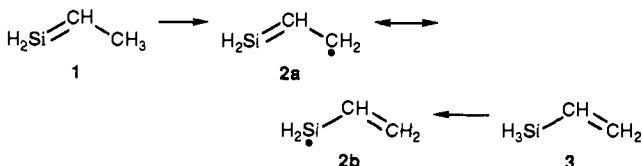
One way to attempt to disentangle possible electronegativity effects of substituents on BDEs from radical stabilizing conjugative effects is to calculate the energetic cost of twisting the substituent out of conjugation.¹ The conjugative stabilization energies (CSE) given in Table II are defined as the energies required to twist the unsaturated group, X, in the X-AH₂[•] radicals out of conjugation with the AH₂[•] radical center. With the exception of H₂C=CH-CH₂[•] and H₂Si=CH-CH₂[•] (vide infra), the CSEs in Table II are within 1 kcal/mol of the relative BDEs. This agreement demonstrates that the major way the unsaturated substituents in Table II affect A-H BDEs is by providing conjugative stabilization for the radicals formed.

The -ΔBDEs in Table II show that unsaturated substituents have a much greater effect on lowering C-H, compared to Si-H, BDEs. Moreover, the CSEs in Table II demonstrate that this difference is due to the fact that unsaturated groups, X, provide much more conjugative stabilization for X-CH₂[•] radicals than for X-SiH₂[•] radicals. These results indicate that, for each substituent group, π bonding to a carbon-centered radical provides more stabilization than does π bonding to a silicon-centered radical.

This conclusion is wholly consistent with the relative strengths of π bonds to carbon and to silicon. The BDEs of π bonds involving carbon and silicon are: π-C=C ≈ 65 kcal/mol,¹⁸⁻²¹ π-C=Si ≈ 35 kcal/mol,^{20,21} and π-Si=Si ≈ 23 kcal/mol.^{21,22} Based on these π BDEs, one would anticipate that the stabilization provided by π bonding to the carbon radical center in X-CH₂[•] would, for all four unsaturated X groups in Table II, exceed that furnished by π bonding to the silicon radical center in X-SiH₂[•].

Allylic Radicals with Different Terminal Groups

1-Silaallyl (2). The significantly greater strength of a C=C π bond, compared to a C=Si π bond, is responsible for the finding that, of the substituents in Table II, the X = H₂Si=CH- group is computed to provide the greatest lowering of the C-H BDE in X-CH₃. Cleavage of a C-H bond in **1** generates allylic radical



2, which can be represented by two resonance structures, **2a** and **2b**. The fact that the latter contains a C=C π bond, instead of the C=Si π bond in the former, suggests that **2b** makes a much larger contribution to the structure of the radical than **2a**. Thus, upon cleavage of a C-H bond in **1**, an allyl radical is formed in which the C=Si π bond in **1** is replaced by a stronger π bond that is largely localized between two carbon atoms.

Several pieces of additional data are in accord with this explanation of why X = H₂Si=CH- lowers the C-H BDE more than any of the other substituents in Table II. For example, if **2b** contributes more than **2a** to the structure of **2**, the H₂C=CH- group in **3** should have little effect on lowering the Si-H BDE in X-SiH₃. In fact, as shown in Table II, X = H₂C=CH- decreases the Si-H BDE by only 0.4 kcal/mol, compared to X = CH₃. The very small effect of vinyl on the calculated BDE

of an adjacent Si-H bond is totally consistent with the experimental finding that phenyl has a negligible effect on the BDE of an adjacent Si-H bond.⁵

The energy required to twist the H₂C=CH- group out of conjugation with the SiH₂[•] radical center in **2** is minimal, amounting to only 0.2 kcal/mol.²³ In contrast, the energy required to twist the H₂Si=CH- group out of conjugation with the CH₂[•] radical center is large, amounting to 31.5 kcal/mol. The difference of 31.3 kcal/mol between the energies required to rotate about the C-C bond and the Si-C bond in **2** is about the same as the difference of 32.6 kcal/mol between the -ΔBDEs in forming **2** from, respectively, **3** and **1**. Not surprisingly, both differences are approximately the same as the difference of about 30 kcal/mol between the strengths of C=C and C=Si π bonds.

From the foregoing discussion, it is easy to understand why in allylic radical **2** the UHF optimized C-C and C-Si bond lengths (1.353 Å and 1.849 Å) are very similar to those (1.325 Å and 1.878 Å) in the same radical with the H₂C=CH- group rotated out of conjugation with the SiH₂[•] radical center. Loss of conjugation also has little effect on the degree of pyramidalization of the SiH₂ group. The SiH₂ pyramidalization angle, φ (the angle between the H-Si-H bisector and the extension of the C-Si bond) increases by only 2.7°, from φ = 48.0° in **2** to φ = 50.7°, when the H₂C=CH- group is rotated out of conjugation.

In contrast, there are, as expected, substantial differences between the C-C and C-Si bond lengths of **2** and those (1.477 Å and 1.700 Å) of the much higher energy radical with the H₂Si=CH- group twisted out of conjugation with the CH₂[•] center. In the latter geometry the existence of a full Si-C π bond also results in complete planarization of the SiH₂ group, while the CH₂[•] center is slightly pyramidalized (φ = 13.0°).

Despite the fact that both energetics and the geometry of **2** indicate that **2b** contributes much more to its structure than **2a**, the calculated unpaired electron densities in **2** suggest some delocalization of unpaired spin from the SiH₂[•] center into the H₂C=CH- group. At the CI-SD level the computed unpaired electron densities at the heavy atoms are 0.94 at silicon, -0.04 at the central carbon, and 0.09 at the carbon of the terminal methylene group. This finding, that the unpaired spin in **2** resides mainly on the SiH₂ group but that positive unpaired spin also appears at the doubly-bonded carbon which is β to it, is in qualitative accord with the experimental results for 1-silaallylic⁶ and 1-silabenzyl⁷ radicals.

In good agreement with the experimental finding that the Si-H hyperfine coupling constant in **2**⁶ is essentially the same as that in CH₃SiH₂[•],²⁴ we calculate the CI-SD unpaired spin density of 0.94 at Si in **2** to be almost the same as the 0.97 that we compute in the methylsilyl radical. However, the size of the C-H hyperfine coupling constant reported for the β carbon in **2**⁶ is indicative of a spin density at this carbon that is roughly three times larger than the value of 0.09 that we calculate at the CI-SD level of theory.²⁵

1,2-Disilaallyl (5). The relative strengths of C=Si and Si=Si π bonds account for the substantial effect of the X = H₂Si=SiH group on the C-H BDE of X-CH₃ (**4**), the very much smaller effect of X = H₂C=SiH on the Si-H BDE of X-SiH₃ (**6**), and

(23) The existence of a barrier to rotating the π bond back into conjugation with the SiH₂[•] center is indicated by the vibrational analysis at the C_v twisted geometry, which finds this geometry to have no imaginary frequencies and, thus, to correspond to a local energy minimum.

(24) Krusic, P. J.; Kochi, J. *J. Am. Chem. Soc.* **1969**, *91*, 3938. Bennett, S. W.; Eaborn, C.; Hudson, A.; Jackson, R. A.; Root, K. D. *J. Chem. Soc. A* **1970**, 348.

(25) Although our population analysis was carried out at the CI-SD level of theory, the geometry for **2** at which it was performed was optimized at the UHF level. Since the UHF wave function for **2** is strongly contaminated by quartet and higher spin states, it is conceivable that the UHF wave function underestimates the amount of π bonding to Si in **2** and thus gives an optimized geometry with Si too pyramidal and/or with too long a C-Si bond. In order to test this possibility, we reoptimized the UHF geometry of **2** with φ at Si constrained to be 20° smaller than at the fully optimized UHF geometry. CI-SD calculations at the constrained geometry did find a 30% increase in the spin density at the terminal methylene group, but the CI-SD energy was 1.5 kcal/mol higher than at the fully optimized UHF geometry.

(17) Hehre, W. J.; Radom, L.; Schleyer, P. v R.; Pople, J. A. *Ab Initio Molecular Orbital Theory*; Wiley: New York, 1986; pp 271-324. For evidence of the accuracy with which relative BDEs can be computed, see: Nicolaides, A.; Borden, W. T. *J. Am. Chem. Soc.* **1991**, *113*, 6750.

(18) Douglas, J. E.; Rabinovitch, B. S.; Looney, F. S. *J. Chem. Phys.* **1955**, *23*, 315.

(19) Benson, S. W. *J. Chem. Educ.* **1965**, *42*, 502. Benson, S. W. *Thermochemical Kinetics*, 2nd ed.; Wiley: New York, 1976; pp 63-65, using the upwardly revised heat of formation for ethyl radical (Parmer, S. S.; Benson, *J. Am. Chem. Soc.* **1989**, *111*, 57 and references cited therein).

(20) Dobbs, K. D.; Hehre, W. J. *Organometallics* **1986**, *5*, 2057.

(21) Schmidt, M. W.; Truong, P. N.; Gordon, M. S. *J. Am. Chem. Soc.* **1987**, *109*, 5217 and references therein.

(22) Hrovat, D. A.; Sun, H.; Borden, W. T. *THEOCHEM* **1988**, *163*, 51.

What is somewhat surprising is that, when the silicon centers in $\text{H}_2\text{Si}=\text{SiH}-\text{SiH}_2^*$ are constrained to be planar, the CSE actually decreases, from 5.6 kcal/mol to 5.0 kcal/mol. This contrasts with the finding for $\text{H}_2\text{Si}=\text{CH}-\text{SiH}_2^*$ and for numerous other molecules studied by us,³⁰ where constraining π bonded atoms to planarity increases the CSE, often substantially. In contrast, constraining the silicons in $\text{H}_2\text{Si}=\text{SiH}-\text{SiH}_2^*$ to planarity raises the energy of the fully conjugated geometry slightly more than the energy of the geometry with one center twisted out of conjugation.

The reason why $\text{H}_2\text{Si}=\text{SiH}-\text{SiH}_2^*$ is exceptional can be traced to the highly pyramidalized geometries at all three silicon centers in the fully conjugated geometry. Despite the increase in π bonding when all three silicons are planarized, planarization of these three centers increases the calculated CI-SD energy by 4.0 kcal/mol. In contrast, in the UHF geometry with one SiH_2 group rotated out of conjugation, only this SiH_2 group is nonplanar.³¹ Planarization of this SiH_2 group, which is calculated to require 3.4 kcal/mol, is energetically more costly than planarization of any of the individual Si centers in the fully conjugated geometry, but 0.6 kcal/mol less costly than simultaneously planarizing all three.

Allyl Radical. With the exception of allyl, for each of the other radicals in Table II, $-\Delta\text{BDE}$ for forming $\text{X}-\text{AH}_2^*$ from $\text{X}-\text{AH}_3$ is the same or slightly larger than the CSE of $\text{X}-\text{AH}_2^*$. Experimentally, the CSE of allyl has been measured to be 15.7 ± 1 kcal/mol,³² which is in excellent agreement with the calculated value of 15.3 kcal/mol in Table II. The experimental value for the CSE of allyl is about 2 kcal/mol greater than the difference between primary C-H BDEs in alkanes³³ and that measured in propene.⁴ The existence of a difference of about this size between the CSE of allyl and $-\Delta\text{BDE}$ for forming allyl is supported by our calculations, which find that the CSE of allyl radical exceeds by 1.4 kcal/mol the reduction of the C-H BDE in $\text{X}-\text{CH}_3$ on replacing $\text{X} = \text{H}_3\text{C}-$ with $\text{X} = \text{CH}_2=\text{CH}-$.

Either the CSE or the $-\Delta\text{BDE}$ can be taken as a measure of the resonance stabilization of the allyl radical, and it can be shown that the values should, in fact, differ.³⁴ The difference between them is equal to the energy change for eq 1, when $\text{X} = \text{CH}_2=\text{CH}-$ is constrained to a geometry in which it cannot conjugate with the unpaired electron. Specifically, the difference of 1.4 kcal/mol in Table II between the CSE for $\text{CH}_2=\text{CH}-\text{CH}_2^*$ and the $-\Delta\text{BDE}$ for $\text{CH}_2=\text{CH}-\text{CH}_3$ means that our calculations find an unconjugated vinyl substituent, X, increases the C-H BDE in $\text{X}-\text{CH}_3$ by 1.4 kcal/mol, relative to $\text{X} = \text{H}_3\text{C}-$.³⁵

The reason for this increase could be due to the operation of one or both of two effects. First, the nominally sp^2 hybridized carbon in a vinyl group is more electron withdrawing than the sp^3 carbon in a methyl group; and this increase in substituent electronegativity would be expected to increase the C-H BDE.¹ Second, the stronger bonds formed by an sp^2 hybridized carbon³⁷

should hyperconjugate less well with an adjacent radical center than do the bonds formed by an sp^3 hybridized carbon and, thus, provide less stabilization for the radical center.

Evidence for the importance of hyperconjugation is found in the results for $\text{H}_2\text{Si}=\text{CH}-\text{CH}_2^*$ in Table II. For $\text{X} = \text{H}_2\text{Si}=\text{CH}-$ in $\text{X}-\text{CH}_3$ comparison of $-\Delta\text{BDE}$ with the CSE shows that, when the π bond in the vinylic group is prohibited from conjugating with the radical center, $\text{X} = \text{H}_2\text{Si}=\text{CH}-$ is computed to decrease the C-H BDE in $\text{X}-\text{CH}_3$ by 1.5 kcal/mol, relative to $\text{X} = \text{CH}_3-$. This contrasts with the finding for nonconjugated $\text{X} = \text{H}_2\text{C}=\text{CH}-$, which, as discussed above, is calculated to increase the C-H BDE in $\text{X}-\text{CH}_3$ by 1.4 kcal/mol, relative to $\text{X} = \text{H}_3\text{C}-$.

It is conceivable that the difference in electronegativity between $\text{X} = \text{H}_2\text{Si}=\text{CH}-$ and $\text{X} = \text{H}_2\text{C}=\text{CH}-$ accounts for part of the 2.9 kcal/mol difference between their effects at nonconjugated geometries on the C-H BDE in $\text{X}-\text{CH}_3$. However, it seems more likely that the bulk of this difference is due to the greater hyperconjugative stabilization of $\text{X}-\text{CH}_2^*$ that is provided by the C-Si σ bond in $\text{X} = \text{H}_2\text{Si}=\text{CH}-$, relative to the C-C σ bond in $\text{X} = \text{H}_2\text{C}=\text{CH}-$.

Support for hyperconjugation, rather than electronegativity, as the major factor in the 2.9 kcal/mol difference between nonconjugating $\text{X} = \text{H}_2\text{C}=\text{CH}-$ and $\text{X} = \text{H}_2\text{Si}=\text{CH}-$ groups on the C-H BDE in $\text{X}-\text{CH}_3$ comes from calculations of the effect on the C-H BDE in $\text{X}-\text{CH}_3$ of the substituent group $\text{X} = \text{H}_3\text{Si}-\text{CH}_2-$. This saturated group decreases the C-H BDE by 2.8 kcal/mol, relative to $\text{X} = \text{CH}_3$. Hyperconjugation, rather than electronegativity, is indicated to be the major source of this reduction, since, when the C-Si bond is oriented orthogonal to the singly occupied orbital on carbon in $\text{H}_3\text{Si}-\text{CH}_2-\text{CH}_2^*$, the energy of the radical increases by 2.2 kcal/mol.³⁹

Hyperconjugation involves the formation of a partial π bond between a radical center and a non-hydrogen atom bonded to it. Due to the much greater strength of C-C, compared to C-Si, π bonds, hyperconjugation is considerably more important in stabilizing $\text{X}-\text{CH}_2^*$ when the atom in X that is bonded to the CH_2^* center is C, rather than Si. The relative unimportance of hyperconjugative stabilization of $\text{X}-\text{CH}_2^*$, when the α atom in the substituent group, X, is Si, explains why replacing $\text{X} = \text{H}_3\text{Si}-$ by twisted $\text{X} = \text{H}_2\text{Si}=\text{SiH}-$ has less than half the effect on lowering the C-H BDE in $\text{X}-\text{CH}_3$ as replacing $\text{X} = \text{H}_3\text{C}-$ with twisted $\text{X} = \text{H}_2\text{Si}=\text{CH}-$.

The importance of hyperconjugation, when it leads to formation of partial C-C π bonds, is what gives twisted $\text{X} = \text{H}_2\text{Si}=\text{CH}-$ and $\text{X} = \text{H}_2\text{C}=\text{CH}-$ groups their unique effects on C-H BDEs. The ability of twisted $\text{X} = \text{H}_2\text{Si}=\text{CH}-$ to hyperconjugate more strongly than any other twisted X group with the radical center in $\text{X}-\text{CH}_2^*$ is responsible for the $-\Delta\text{BDE}$ for this group exceeding its CSE by more than that of any other group. Similarly, we attribute the fact that the $-\Delta\text{BDE}$ for formation of allyl radical is actually smaller than its CSE to the poorer ability of twisted $\text{X} = \text{H}_2\text{C}=\text{CH}-$, compared to $\text{X} = \text{H}_3\text{C}-$, to hyperconjugate with the radical center in $\text{X}-\text{CH}_2^*$.

(30) Sun, H.; Hrovat, D. A.; Borden, W. T. *J. Am. Chem. Soc.* **1987**, *109*, 5275. Wang, S. Y.; Borden, W. T. *J. Am. Chem. Soc.* **1989**, *111*, 7282. Coolidge, M.; Borden, W. T. *J. Am. Chem. Soc.* **1990**, *112*, 1704. Hammons, J. H.; Coolidge, M.; Borden, W. T. *J. Phys. Chem.* **1990**, *94*, 5468. Hammons, J. H.; Hrovat, D. A.; Borden, W. T. *J. Phys. Org. Chem.* **1990**, *3*, 635.

(31) A UHF vibrational analysis found only one imaginary frequency at this C₂ geometry, corresponding to SiH_2^* rotation.

(32) Korth, H.-G.; Trill, H.; Sustmann, R. *J. Am. Chem. Soc.* **1981**, *103*, 4483.

(33) Parmar, S. S.; Benson, J. *Am. Chem. Soc.* **1989**, *111*, 57 and references cited therein. Ruscic, B.; Berkowitz, J.; Curtiss, L. A.; Pople, J. A. *J. Chem. Phys.* **1989**, *91*, 114.

(34) Doering, W. von E.; Roth, W. R.; Breuckmann, R.; Figge, L.; Lennartz, H.-W.; Fessner, W.-D.; Prinzbach, H. *Chem. Ber.* **1988**, *121*, 1.

(35) EPR studies of pentadienyl radical³⁶ find that its CSE, relative to a localized radical and two, nonconjugated vinyl groups, is about 25 kcal/mol. This CSE exceeds the C-H $-\Delta\text{BDE}$ of about 19 kcal/mol for the two vinyl groups in 1,4-pentadiene.^{4,36} Thus, two nonconjugated vinyl groups appear to increase the BDE for the secondary C-H of 1,4-pentadiene by about 6 kcal/mol, a value that is probably well in excess of the combined experimental errors in the CSE of pentadienyl and the $-\Delta\text{BDE}$ for 1,4-pentadiene.

(36) MacInnes, I.; Walton, J. C. *J. Chem. Soc., Perkin Trans. 2* **1985**, 1073. Clark, K. B.; Culshaw, P. N.; Griller, D.; Lossing, F. P.; Simoes, J. A. M.; Walton, J. C. *J. Org. Chem.* **1991**, *56*, 5535.

(37) The C-H BDE of ethylene³⁸ exceeds that of ethane³³ by about 10 kcal/mol.

(38) Ervin, K. M.; Gronert, S.; Barlow, S. E.; Gilles, M. K.; Harrison, A. G.; Bierbaum, V. M.; DePuy, C. H.; Lineberger, W. C.; Ellison, G. B. *J. Am. Chem. Soc.* **1990**, *112*, 5750.

(39) This finding of an energetic preference for a conformation in which the C-Si bond can hyperconjugate with the singly occupied orbital is in agreement with experiments⁴⁰ and with the results of previous calculations.⁴¹ In contrast, both experiments⁴⁰ and calculations⁴¹ find a much smaller conformational preference in the 1-propyl radical, and the conformation in which the C-C bond to the β -methyl group is orthogonal to the singly occupied orbital at the terminal carbon is apparently favored.^{40,41b} It is not surprising, therefore, that we calculate the BDE of the primary C-H bond in propane to differ insignificantly from that in ethane.

(40) Krusic, P.; Kochi, J. *J. Am. Chem. Soc.* **1971**, *93*, 846. Krusic, P. J.; Meakin, P.; Jesson, J. P. *J. Phys. Chem.* **1971**, *75*, 3438.

(41) (a) Bernardi, F.; Bottoni, A.; Fossey, J.; Sorba, J. *Tetrahedron* **1986**, *42*, 5567. (b) Ibrahim, M. R.; Jorgensen, W. L. *J. Am. Chem. Soc.* **1989**, *111*, 819.

(42) Planar equilibrium geometries have also been found computationally for 2-silaallyl cation and anion: Rajca, A.; Streitwieser, A. *Organometallics* **1988**, *7*, 2215.

Acknowledgment. We thank the National Science Foundation for support of this research and for a grant that allowed purchase of the Convex C-2 computer, on which some of these calculations were performed. We also thank the San Diego Supercomputer Center for a generous allocation of computer time.

Supplementary Material Available: Tables of the RHF optimized geometries and energies of the closed shell molecules and the UHF geometries and energies of the radicals that appear in Table I (3 pages). Ordering information is given on any current masthead page.

An ab Initio MO Study on Ethylene and Propylene Insertion into the Ti–CH₃ Bond in CH₃TiCl₂⁺ as a Model of Homogeneous Olefin Polymerization

Hiroshi Kawamura-Kuribayashi,^{†,‡} Nobuaki Koga,[†] and Keiji Morokuma^{*†}

Contribution from the Institute for Molecular Science, Myodaiji, Okazaki 444, Japan, and Chiba Research Laboratory, Sumitomo Chemical Co., Ltd., 2-1 Kitasode Sodegaura Chiba 299-02, Japan. Received April 11, 1991

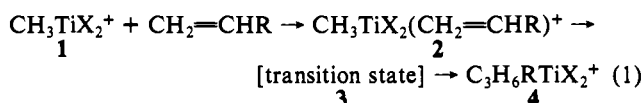
Abstract: As a model of olefin polymerization by a homogeneous Ziegler–Natta catalyst, the mechanism of the insertion reaction of ethylene and propylene into CH₃TiCl₂⁺ has been studied by the ab initio MO method. The structures of the reactant, the intermediate, the transition state, and the product have been optimized with the RHF/3-21G (Ti:MIDI4) method. The transition state is four-centered and is slightly nonplanar to avoid C–H bond eclipsing. In the product strong C^β–C^γ and C–H agostic interactions take place to donate electrons to Ti vacant d orbitals. The energetics calculated at the unrestricted second-order Møller–Plesset perturbation level with double spin projection (DPUMP2) shows that the reaction proceeds via an ethylene complex with a binding energy of 45 kcal/mol and through the transition state with an activation energy from the ethylene complex of about 4 kcal/mol. In propylene polymerization, the barrier is higher than in ethylene insertion, and the primary insertion is easier than the secondary insertion, both consistent with experiments. The energy decomposition analysis indicates that these chemo- and regioselectivities are controlled by electrostatic and exchange (steric) interactions. The nonplanarity of the transition state makes one of two stereospecific primary insertion pathways substantially more favorable than the other; this tendency of a nonplanar transition state may have significance in determining stereospecificity in olefin polymerizations.

I. Introduction

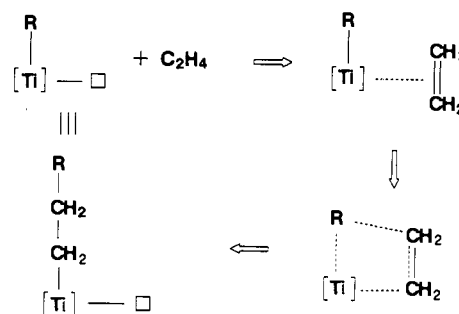
The discovery of Ziegler–Natta polymerization in 1953 is one of the most important achievements in the field of synthetic polymer chemistry during the past half-century. For this olefin polymerization, a heterogeneous as well as homogeneous catalyst has been adopted. Heterogeneous catalysts are usually transition metal halides with cocatalysts such as aluminum alkyl compounds and electron donors; an example of such a combination studied experimentally very extensively is TiCl₃ + (C₂H₅)₂AlCl + aromatic ester.^{1–5} Homogeneous catalysts, on the other hand, are metallocenes,^{6–9} transition metal dihalide dialkoxides¹⁰ (e.g., (RO)₂TiCl₂), and metal tetraalkyls,^{11,12} which are soluble in hydrocarbon solvent.

The mechanism proposed by Cossee¹³ has been accepted widely as the most plausible, though it is very generic and qualitative. This mechanism is illustrated for Ti in Scheme I. The first step is olefin coordination to a vacant site of Ti. In the second step olefin inserts into the Ti–C bond through a four-membered cyclic transition state. This newly grown alkyl Ti species reinitiates olefin coordination and thus the propagation step.

Based on this mechanism, many MO theoretical studies have been carried out for this catalytic system.^{14–24} In the earliest ab initio MO study, Novaro, Clementi, and co-workers²⁰ calculated the energy profile and analyzed briefly the electronic structure for each step of this mechanism with assumed geometries. Fujimoto and co-workers used a model cationic reaction (eq 1) with



Scheme I



X = Cl for ethylene insertion (R = H) and optimized the transition structure with the ab initio restricted Hartree–Fock (RHF) method

- (1) Keii, T. *Kinetics of Ziegler–Natta Polymerization*; Kodansha: Tokyo, 1972.
- (2) Boor, J., Jr. *Ziegler–Natta Catalysts and Polymerization*; Academic Press: New York, 1979.
- (3) Kissin, Y. V. *Isospecific Polymerization of Olefins*; Springer-Verlag: New York, 1985.
- (4) Allen, G. B. *Comprehensive Polymer Science*; Pergamon Press: Oxford, 1989.
- (5) Choi, K.; Ray, W. H. *Rev. Macromol. Chem.* **1985**, C25, 1, 57.
- (6) Ewen, J. A. *J. Am. Chem. Soc.* **1984**, 106, 6355.
- (7) Kaminsky, W.; Kulper, K.; Brintzinger, H. H.; Wild, F. R. W. P. *Angew. Chem., Int. Ed. Engl.* **1985**, 24, 507.
- (8) Ewen, J. A.; Jones, R. L.; Razavi, A.; Ferrara, J. D. *J. Am. Chem. Soc.* **1988**, 110, 6255.
- (9) Miya, S.; Mise, T.; Yamazaki, H. *Chem. Lett.* **1989**, 1853.
- (10) Miyatake, T.; Mizunuma, K.; Seki, Y.; Kakugo, M. *Makromol. Chem., Rapid Commun.* **1989**, 10, 349.
- (11) Ballard, D. G. H.; Van Lienden, P. W. *Makromol. Chem.* **1972**, 154, 177.
- (12) Ballard, D. G. H.; Dawkins, J. V.; Key, J. M.; Van Lienden, P. W. *Makromol. Chem.* **1973**, 165, 173.

[†]Institute for Molecular Science.

[‡]Sumitomo Chemical Co., Ltd.